

# Impact Resistance of Deflection-Hardening Fiber Reinforced Concretes with Different Mixture Parameters

## Running Head (Short Title): Impact Resistance of HPFRCs with Coarse Aggregates

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### ABSTRACT

The impact behavior of deflection-hardening High Performance Fiber Reinforced Cementitious Concretes (HPFRCs) was evaluated herein. During the preparation of HPFRCs, fiber type and amount, fly ash to Portland cement ratio and aggregate to binder ratio were taken into consideration. HPFRC beams were tested for impact resistance using free-fall drop-weight test. Acceleration, displacement and impact load vs. time graphs were constructed and their relationship to the proposed mixture parameters were evaluated. The paper also aims to present and verify a nonlinear finite element analysis, employing the incremental nonlinear dynamic analysis, concrete damage plasticity model and contact surface between the dropped hammer and test specimen available in ABAQUS. The proposed modelling provides extensive and accurate data on structural behavior, including acceleration, displacement profiles and residual displacement results. Experimental results which are further confirmed by numerical studies show that impact resistance of HPFRC mixtures can be significantly improved by a proper mixture proportioning. In the presence of high amounts of coarse aggregates, fly ash and increased volume of hybrid fibers, impact resistance of fiberless reference specimens can be modified in a way to exhibit relatively smaller displacement results after impact loading without risking the basic mechanical properties and deflection-hardening response with multiple cracking.

**Keywords:** high performance fiber reinforced concrete (HPFRC), deflection-hardening, impact, coarse aggregate, fly ash, abaqus.

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## 1. INTRODUCTION

Conventional concrete is the most widely used construction material in the world although it is relatively brittle. To account for the high brittleness of conventional concrete materials, High Performance Fiber Reinforced Concretes (HPFRCs) have been manufactured in the last few decades. HPFRCs are characterized by their dominant performance in accounting for tensile forces/strain and crack occurrence/propagation. According to previous studies, the increased crack bearing ability of HPFRCs due to strain and/or deflection-hardening behavior offsets many common durability concerns.<sup>1-4</sup> Given the materials' enhanced performance, many studies have focused on their basic mechanical and durability properties.<sup>5-7</sup> Due to the crack bearing ability and controlled cracking behavior of HPFRCs, their self-healing behavior has also been studied extensively.<sup>8-10</sup> However, studies into more complex material properties such as resistance to impact loading are lacking in the current literature. Thus, studying the impact resistance of HPFRC mixtures, especially those characterized by deflection-hardening behavior is believed to make a valuable contribution for the current literature.

When under the influence of impact loads, conventional concrete materials fail in tensile mode with a softening response after reaching to peak point, given their quasi-brittle nature.<sup>11-22</sup> There is no established standards or methods for impact testing in recent studies.<sup>23-26</sup> However, ASTM E23 regulations improved the test setup performance significantly and gave good starting point for the limits of impact experiments.<sup>27</sup> Experimental impact studies in literature are generally categorized into two main segments. One of them depends on the investigation of specimens under impact loads that are applied by test equipments. These types of studies are concentrated mostly on steel materials. Other studies use equipment with mechanisms that drop masses from height. This method is mostly used for the impact testing of concrete.<sup>28,29</sup> Similarly, here, an impact test setup that was designed by the authors and drops a constant weight from a height was used for testing of HPFRC specimens.

According to Maalej et al.<sup>30</sup>, there is a clearer relationship between impact resistance and tensile strength than that between impact resistance and compressive strength of concrete. It was also concluded that structural elements manufactured with Engineered Cementitious Composites (ECC) (a relatively appealing branch of HPFRCs) characterized by strain-hardening response and multiple microcracking behavior under tensile/shear loads can enhance impact behavior considerably.<sup>30</sup> It may be thus stated that impact resistance can be improved by delaying the crack formation through strain/deflection-hardening response accompanied by multiple microcracking and enhancing the strength in tension.

In many types of HPFRC mixtures, including ECC, the amount and maximum size of coarse aggregates are restricted to achieve strain/deflection-hardening response. One reason for that is the non-uniform distribution of individual fibers in the presence of high amounts of coarse aggregates. When aggregates with larger than the average particle sizes are used, spacing of individual fibers causes inadequate dispersion/balling, with the balling effect being more pronounced with increased maximum aggregate size.<sup>31</sup> Generally, an increase in the size of aggregate particles causes more clumping and greater interaction of the fibers.<sup>32</sup> Another reason for not using coarse aggregates is associated with the increased matrix fracture toughness values in the presence of coarse aggregates which increases the fracture toughness of the brittle matrix and significantly lowers the ductility of ultimate material.<sup>33</sup> The influence of both of these factors is likely to exacerbate when mixtures are reinforced with more than one type of fiber with varying properties. Thus, HPFRCs are generally manufactured with relatively small-size aggregates, regardless of the selected fiber system (single or hybrid).<sup>34,35</sup> While preparing HPFRC mixtures, the use of small aggregates is beneficial in uniform distribution of fibers, although this also increases the Portland cement amount as the main binder which is not cost-effective and more detrimental to dimensional stability than systems incorporating coarse aggregates. To reduce the chance of dimensional instability and overall cost of HPFRC systems, cement is commonly replaced with industrial by-products (e.g. fly ash [FA], slag etc.). Lower toughness values can be acquired with the use of such by-products which may favor the materials' ductility even in the presence of coarse aggregates.<sup>32</sup>

Few studies have targeted the development of HPFRC mixtures with strain/deflection-hardening capability incorporating coarse aggregates.<sup>36,37</sup> In a recent study by the authors, deflection-hardening HPFRC mixtures with single and hybrid fibers were developed using different amounts of FA and coarse aggregates with a maximum size of 12 mm.<sup>7</sup> Although the basic mechanical properties (compressive strength, flexural strength and mid-span beam displacement) of HPFRC mixtures manufactured in the cited study were notable, studies detailing the impact performance of such materials are limited.<sup>16,38-41</sup> Moreover, to the authors' best knowledge, there are no studies available in the literature dealing with the impact performance of deflection-hardening HPFRC mixtures in the presence of large amounts of coarse aggregates. To fill that knowledge gap, a follow-up study to that of Banyhussan et al.<sup>7</sup> was undertaken, focusing mainly on the impact resistance of previously developed HPFRC mixtures with deflection-hardening capability. Beam specimens of different HPFRC mixtures were produced and tested for their impact resistance after free-fall drop-weight tests. HPFRCs were produced by taking the type and amount of fibers, FA to

Portland cement ratio (FA/PC) and aggregate to binder ratio (A/B) into account. To observe the possible effects of these parameters on the impact performance, 24 beams were tested. Tested beam specimens were modelled in a finite element program (ABAQUS), incremental nonlinear dynamic analysis was performed, and the effectiveness of the developed finite element model in reflecting the impact behavior of HPFRC beam specimens was investigated.

## **2. EXPERIMENTAL PROGRAM**

To characterize the impact behavior of HPFRCs,  $50 \times 50 \times 750 \text{ mm}^3$  beam specimens were produced without any steel rebars. Table 1 shows the experimental variables taken into consideration. While preparing the mixtures, the type/amount of fibers, FA/PC and A/B ratios were selected as variant parameters. Three fiber types, FA/PC ratio and A/B ratio were chosen. Beam specimens produced with 24 different mixtures were then tested for their impact resistance using free-fall drop-weight testing with a specific impact loading.

### **2.1 Materials and mixture proportions**

CEM I 42.5R ordinary Portland cement (PC), FA with lime content of 9.8% and silica fume (SF) were used for the production of HPFRC mixtures. The total SF amount used was constant at 7% of PC weight. Surface areas of PC, FA and SF were 325, 290, and 19080  $\text{m}^2/\text{kg}$ , respectively. Particle size distributions of the raw materials can be found in Ref. <sup>7</sup>.

Mixtures were produced with three FA/PC ratios (0.20, 0.45 and 0.70) and fine and coarse aggregates. Fine aggregate was river sand with fineness modulus of 2.67 and coarse aggregate was crushed limestone with maximum aggregate size of 12 mm. To find the well-graded aggregate combination, 0.45 power chart method using the Fuller formula was adopted and a gradation curve closest to the maximum density curve was obtained. Combined aggregate gradation was achieved using 57% fine and 43% coarse aggregates, by weight. Mixtures' total aggregate (coarse + fine) to binder (PC + FA + SF) ratios (A/B) were 1.0, 1.5 and 2.0. Polycarboxylate-ether-based high range water reducing admixture (HRWRA) was also used to achieve desired workability. Mixtures produced with different FA/PC and A/B ratios and amounts/types of fibers required different HRWRA amounts to obtain uniform fiber distribution and nearly self-compacting properties. Fresh properties of HPFRC mixtures were measured using slump test. After slump tests, average slump flow measurements were made. Depending on the mixture type, slump flows ranged between 660-700 mm. Polyvinyl-alcohol (P), hooked-end steel (S), nylon (N) fibers were used. P fibers were with length of 18 mm, diameter of 0.20 mm, tensile strength of 1000 MPa, elastic modulus of 29 GPa and specific gravity of 1.30. S fibers were with length of 30 mm, diameter of 0.75 mm, tensile strength of

1100 MPa, elastic modulus of 200 GPa and specific gravity of 7.30. N fibers were with length of 19 mm, diameter of 0.05 mm, tensile strength of 966 MPa, elastic modulus of 25 GPa and specific gravity of 1.14. A moderate fiber volume ( $\leq 2\%$ ) was used in all HPFRC mixtures.

24 HPFRC mixtures were produced with constant water to binder ratio (W/B) of 0.40. Ingredients used for the production of all mixtures are tabulated in Table 1 showing that several letters and numbers were used for denomination. For example, in the 16<sup>th</sup> mixture (P0.5S1N0.5\_0.20\_1.0), P, S and N fibers were used by 0.5%, 1.0% and 0.5% of total mixture volume, respectively and 0.20 and 1.0 stand for FA/PC and A/B ratios, respectively.

Selection of different FA/PC and A/B ratios and fiber types/amounts were made based on the experience of authors from a recent study.<sup>7</sup> In the cited study, preliminary tests on variety of HPFRC mixtures were performed using different FA/PC and A/B ratios together with fiber types/amounts. The selected proportions and ingredients were then decided depending on the achievement of optimal mechanical properties and deflection-hardening response coupled with multiple microcracking in the presence of as much coarse aggregates as possible.

## **2.2 Mixing, sample preparation and testing**

A 40-liter-capacity pan-type concrete mixer was used to manufacture mixtures, following the same procedures. The mixing steps of HPFRC mixtures were discussed in detail in Ref. <sup>7</sup>. Beam specimens measuring  $50 \times 50 \times 750 \text{ mm}^3$  were produced for testing of flexural impact resistance under free-fall drop-weight testing. In addition to the impact tests, mechanical properties (compressive strength, flexural strength and displacement) of different HPFRC mixtures were tested. Details of specimen dimensions and testing procedures related to basic mechanical properties of mixtures can be found in Ref. <sup>7</sup>. Different from the specimens of mechanical property characterization in cited study, here, dogbone-shaped specimens were produced as well for uniaxial tensile tests, and the results obtained from these tests were used as raw data in numerical analysis along with the compressive strength test results. Considering the use of coarse aggregates in HPFRC mixtures, the geometry of dogbone-shaped specimens were selected in accordance with Ref. <sup>42</sup>. Uniaxial tensile testing was conducted at a loading rate of 0.1 mm/min, and load and elongation results were recorded. Elongation was measured using two linear variable displacement transducers (LVDTs) attached to both sides of the central portion of dogbone-shaped specimens. Uniaxial tensile measurements were taken from  $30 \times 30 \text{ mm}^2$  cross-sectional dimensions of dogbone specimens.<sup>42</sup> All tests performed in this study were implemented after 28 days and details of the curing procedures were the same for all proposed specimens and explained in Ref. <sup>7</sup>.

## 2.3 Test setup and instrumentation

Impact loads were applied via test setup, details of which are provided in Figure 1. The test setup itself allows weights of varying magnitudes to be dropped from a maximum height of 2500 mm onto specimens of varying dimensions. The weight and drop height of the hammer were kept constant during the experiment; a 9 kg hammer was dropped from a height of 600 mm to create impact loading from the same contact point for different beam specimens. High-strength  $50 \times 50 \times 4 \text{ mm}^3$  steel plates were placed on the contact points to prevent local fractures from the contact point and achieve distributed loading. Steel plates on which loading were applied were fixed to specimens with a mechanical anchor. A piece of rubber was placed between the plates and specimens to prevent stress localization due to surface roughness.

Hammer weight, drop height and impact energy level were selected accordingly to best trace the damage occurrence. The capacity of dynamic accelerometers and load cell were also considered during hammer weight and drop height selection. Special attention was paid in selection these two parameters to avoid very high energy impact, which can lead to exceedance of sensor limits and sudden, substantial damage introduction to specimens. To avoid these problems, levels of impact loads were limited to 52.97 J ( $600 \text{ mm} \times 9.81 \text{ m/sec}^2 \times 9.0 \text{ kg}$  [height of drop weight  $\times$  gravitational acceleration  $\times$  mass of drop weight]). Accelerations at two symmetrical points were measured to observe the effects of impact loading. Accelerometers were placed symmetrically 150 mm away from the point of impact loading and fixed with brass connections using mechanical anchors. Displacements were measured using two LVDTs placed symmetrically 50 mm away from the point of impact.

Figure 2 shows the view and layout of beam specimen ready for impact resistance testing. A dynamic data collection system with specifically designed software was used to properly save impact testing data. The loading created by the drop hammer was measured using a dynamic load cell. Impact velocity of the drop hammer was calculated by a speedometer placed on top of the hammer, and average of measured impact velocities of beam specimens was 3.5 m/s. These values, measured from different specimens, were very close to each other. Identical impact loading was applied to all specimens. The accelerometers and LVDTs were connected to the data logger with computerized software to record acceleration-time, displacement-time and impact load-time graphs after applying the impact load.

## 3. RESULTS AND DISCUSSION

### 3.1 Basic mechanical properties

In this section, compressive strength, flexural strength and flexural displacement results of HPFRCs are evaluated. For each mechanical property, six specimens were tested and average results are presented in Table 1. Individual test results of specimens for each test were generally close to each other, with a coefficient of variation (COV) less than 5%. Since the main topic of the present paper is to assess the impact behavior of newly-developed HPFRC mixtures, only a brief discussion of basic mechanical property results is presented below and further details on the related topic can be found in the companion paper.<sup>7</sup>

Increasing the amount of FA in mixtures having constant A/B ratio and fiber types/amounts resulted in lower compressive strength. Observed behavior was associated with significantly lower cementing capability of FA retarding the attainment of higher strengths. Irrespective of the amount of FA used in the mixtures, utilization of different types of fibers led limited increments (10%), indicating the slight contribution of fiber reinforcement on the compressive strength although the same is not true for flexural parameters (as will be detailed). Comparing the results of specimens with the same fiber combinations and FA/PC ratios, higher A/B ratios increased the compressive strength results. This finding was attributed to the tortuosity of cracking path increasing the ultimate energy absorption capacity at final failure.<sup>7</sup>

For specimens with the same A/B ratio, increasing the amount of FA generally reduced the flexural strength results. This was related with the factors reducing the compressive strength results.<sup>7,43</sup> When similar FA/PC ratios and fiber types/amounts were selected, increasing A/B ratios evidently increased the flexural strength results. Similar to compressive strength results, this was attributed to the effect of higher coarse aggregate amounts increasing the tortuosity of cracking path until failure. Another explanation for this behavior could be the influence of significantly high amounts of FA utilization in HPFRC systems improving workability, fiber distribution and staying intact for longer periods to be hydrated. Flexural strength results were considerably improved with the addition of fibers into HPFRCs (Table 1 and Figure 3). To exemplify, addition of only 1% of S fibers (by volume) into reference mixtures with no fibers, 36% of improvement in average flexural strength results was achievable.

Average flexural displacement results varied based on different FA/PC ratios although there was a general increasing trend in the values with increased FA amounts (Table 1). Beneficial effects of FA utilization on flexural displacement results were related with the capability of FA particles reducing the chemical bonding between synthetic fibers and matrix, fracture toughness and increasing frictional bonding in interface.<sup>44</sup> Another possible cause of this general trend can be the spherical morphology of FA particles favoring uniform fiber distribution.<sup>45</sup> Increasing the A/B ratio of mixtures did not make any negative effect on

flexural displacement suggesting that ductility can be modified with the use of proper amounts of FA even in the presence of high amounts of coarse aggregates.<sup>34</sup> Fiber reinforcement was quite influential on flexural displacement results irrespective of FA/PC and A/B ratios. Although this was monitorable from Table 1, clearer comparisons can be made from Figure 3 which confirms significant improvements in both flexural strength and displacement results. Deflection-hardening response was also confirmed, since all mixtures with different types/amounts of fibers showed peak load and corresponding flexural displacement results greater than their first cracking load and its corresponding flexural displacement recorded at the first cracking load.<sup>46</sup> All specimens showed multiple microcracks, which is a direct consequence of deflection-hardening under bending (Figure 3).

### **3.2 Impact behavior**

Impact performances of HPFRCs were analyzed by evaluating data related to impact load vs. time, acceleration vs. time and displacement vs. time graphs. Representative acceleration, displacement and impact load vs. time graphs are shown in Figure 4, 5 and 6, respectively. In Table 2, the maximum acceleration (for left/right points), displacement (for left/right points) and impact load results are summarized.

#### **3.2.1 Effect of fibers**

Addition of fibers into HPFRC beams was very effective on impact performance and led to significant increments in acceleration results and decrements in displacement results depending on the type/amount of fibers. For specimens with an A/B ratio of 1.0, the average of left and right acceleration results for specimens having only S fibers was 33% higher than that of reference specimens without fibers, while the average displacement results was 23% lower. For specimens having S and P fibers at the same A/B ratio, the average of left and right acceleration results was 23% higher, and the average displacement was 23% lower compared to reference specimens. In mixtures with all three fiber types, the average of acceleration and displacement results were 29% higher and 42% lower than the reference specimens, respectively. These results clearly show that regardless of the type/amount, fibers improve the impact resistance of conventional concrete material for a given FA/PC and A/B ratio suggesting a more rigid behavior, higher residual impact capacity and endurance to impact loads. When impacted, frontal face of a beam specimen where the impact energy is introduced is subjected to the waves of compressive stress while the free distal (back) face is subjected to the waves of tensile stress (as the reflection of waves of compressive stress at the frontal face). It can thus be stated that specimens should be with adequate compressive strength in



order not to crush and/or fail from the frontal face and should also be with adequate tensile strength to enhance the impact performance at the distal face.<sup>47</sup> According to Table 1, addition of S fibers did not make a marked contribution to compressive strength results of control specimens and failure took place because of the formation and localization of a single crack at the distal face of both reference and S-fiber-reinforced beams although this was much clearer for reference specimens (Figure 7). For the imposed impact energy, compressive strength of HPFRC beams were adequate to prevent crushing/failure from the frontal face although this was not the case for the flexural strength (especially for reference specimens). However, utilization of even 1% of S fibers in reference specimens did make a substantial contribution to impact performance by significantly favoring the flexural properties (Table 1 and Figure 7). All HPFRC mixtures (excluding reference mixtures numbered from 1 to 3) produced herein are characterized with deflection-hardening response through multiple microcracking (Figure 3).<sup>7</sup> Significantly higher damage tolerance of HPFRC specimens with different type/amount of fibers than reference specimens allow them to absorb more flexural impact energy while better maintaining the overall integrity of specimens as seen from Figure 7.

Increased volume of fibers also enhanced the flexural impact resistance of HPFRC beams (Table 2, Figure 4 and 5). In the studies of Mao et al.<sup>48</sup> and Barnett et al.<sup>49</sup> where the blast resistance of Fiber-Reinforced Ultra-High Performance Concrete (FR-UHPC) slabs was studied, similar results were reported and concluded that increased post-cracking tendency and deflection-hardening response (obtained from some of the specimens) lends FR-UHPFC specimens high flexural energy absorption capacity. According to Figure 2, increasing the fiber volume of HPFRC mixtures from 1 to 2%, by volume led deflection-hardening response to be more pronounced (detailed discussions can be found in Ref. <sup>7</sup>) and flexural toughness capacity (area under the plastic region of flexural stress-displacement plot) to be higher which can explain the enhanced impact resistance monitored at higher dosages of fiber reinforcement. Another reason for the observed improvements in the impact resistance of HPFRC mixtures at higher fiber dosages can be due to further improvements took place in the compressive strength results although they are limited (Table 1). It is likely that slightly increased compressive strength results at higher fiber dosages may lead to partial damping of impact load at the frontal face and reduction of the impact effect at the distal face. Moreover, at the same fiber dosage (2%, by volume), FA/PC ratio and A/B ratio, there were further improvements in flexural impact resistance of HPFRC specimens when fibers were hybridized (Figure 7). For example, average of left and right displacements of P0.5S1N0.5\_0.20\_1.0 mixture was 18.3 mm after impact loading while the same value was

26.8 mm for P1S1N0\_0.20\_1.0 mixture. A similar behavior was also noted for mixtures with different FA/PC and A/B ratios (Table 2). Although the compressive strength, flexural parameters, toughness of HPFRC specimens with two (S, P) or three (S, P, N) different fibers were close (Table 1 and Figure 3), clear differences were noted in displacement and acceleration results of these specimens after the application of impact loading. This behavior could be related with the advantages of using N fibers instead of P fibers. Fracturing in concrete is a mechanism with multi-scale nature<sup>50</sup> which means that it needs to be tackled by addressing cracking occurrences at different scales. Individual properties of P and N fibers are very close excluding their diameter which is 0.20 mm for P and 0.05 mm for N fibers. Therefore, it might have been possible for N fibers to bridge smaller microcracks than P fibers and contribute more to the flexural impact resistance of HPFRC mixtures by improving the materials' behavior before and/or right after the cracking formation. Additionally, nylon swells upon moisture uptake of amide chains ( $-\text{CO}-\text{NH}-$ ) of N fibers<sup>51</sup> and its bonding to polymer backbone improving stiffness and allowing greater capacity for tensile stresses<sup>52</sup> which may also improve the impact resistance. Relatively cheaper N fibers can therefore be replaced with P fibers safely by half of volume in favor of enhancing flexural impact resistance without sacrificing the basic mechanical properties of HPFRC mixtures.

Another factor that can be influential on the impact performance of HPFRC mixtures is the orientation and uniform distribution of individual fibers which are affected by the mixtures' processing/casting procedure and specimen/structural dimensions.<sup>53</sup> For example, by changing the distribution of fibers from 1D uniform alignment to 3D random distribution, load carrying capacity of a composite can be reduced by 20%.<sup>54</sup> Likewise, flexural impact load carrying capacity of HPFRC mixtures can be modified by changing the orientations of individual fibers especially within the impact zone. It is expected that the fibers incorporated in HPFRC mixtures produced herein are 2D-oriented due to limited cross-section ( $50 \times 50 \text{ mm}^2$ ) of beams. 2D-oriented distribution of fibers results in higher tensile stress and bridging capacity than 3D-oriented distribution (e.g. in the case of specimens with larger dimensions such as beams and columns). Increased bridging capacity improves the ductility by increasing the range of flaw sizes.<sup>55</sup> Increments in fiber volume and replacement of P fibers with N fibers may have played a role in changing the overall orientation of fibers within the limited cross-section of beam specimens where impact load was applied and as a result improved the impact performance. However, it needs to be stated that this explanation requires further clarification by testing of specimens with different sizes and techniques (e.g. fluorescence microscopy and digital image analysis)<sup>56</sup> which is beyond the scope of current paper.

### 3.2.2 Effect of aggregate content

The second variable of the experimental program was A/B ratio. A rigorous comparison regarding the A/B ratio and its effects on the impact performance of HPFRC mixtures can only be made considering mixtures with the same fiber type/amount and FA/PC. Therefore, mixtures numbered from 7 to 15 and 16 to 24 were compared among themselves. For example, average of left and right displacements for P1S1N0\_0.20\_1.0, P1S1N0\_0.20\_1.5 and P1S1N0\_0.20\_2.0 mixtures were noted to be -26.8 mm, -30.3 mm and -31.5 mm, respectively. Same results for P1S1N0\_0.20\_1.0, P1S1N0\_0.20\_1.5 and P1S1N0\_0.20\_2.0 mixtures were -18.2 mm, -21.8 mm and -24.6 mm, respectively following a similar incremental trend (Table 2). These results therefore suggest that increased amounts of coarse aggregates in the case of hybrid-fiber reinforced HPFRC mixtures led impact resistance to decrease although rates of decrement were not that dramatic.

In accordance with the literature, concrete mixtures outperform paste mixtures in terms of impact resistance given their higher energy need to cause final fracture.<sup>28</sup> Likewise, it was anticipated that increasing the amount of coarse aggregates would also result in increased impact performance of HPFRC mixtures thanks to increased toughness, modulus of elasticity and cracking tortuosity. However, it seems that different from incorporating coarse aggregates into pastes, increasing the amount of coarse aggregates in the presence of hybrid fibers clearly differs from the perspective of impact resistance. Authors have previously shown that the HPFRC mixtures produced in this study were with similar elastic modules and toughnesses (according to their flexural stress – deflection graphs) irrespective of the selected A/B ratios.<sup>7</sup> Therefore, these parameters (elastic modulus and toughness) which are likely to change with the changes in the amount of coarse aggregates and be influential on the impact performance of HPFRCs were not considered to have paramount effect on the overall observed behavior. Rather than these parameters, it is believed that effects of coarse aggregates on the flexural ductility and rapid extension of cracks available in the interfacial transition zones (ITZs) between the coarse aggregates and cementitious paste are more pronounced on the impact performance of HPFRC mixtures with hybrid fibers. As can be seen from Table 1, generally, there were reductions in the flexural displacement results with the increased A/B ratios for a given fiber type and FA/PC although deflection-hardening response was still guaranteed for all HPFRC mixtures.<sup>7</sup> This might be one of the reasons for reduced impact resistance of mixtures with higher amounts of coarse aggregates. Under impact loading, (different from slow-motion compressive and flexural loading discussed in Section 3.1) specimens are stressed very rapidly which forces large number of microcracks available especially within

the ITZs and cementitious paste to extent very rapidly. Hence, it is very likely for these cracks to be forced to propagate through the coarse aggregates rather than travelling around them.<sup>57-59</sup> This may eliminate the role of coarse aggregates to act like barriers to rapid crack propagation and reduce the impact resistance of HPFRC mixtures as well.

### **3.2.3 Effect of fly ash content**

As the amount of FA increased, acceleration results increased while displacement results decreased. This finding was observed in all proposed HPFRC mixtures, with and without different fiber combinations. In the reference HPFRC beam specimens, when FA/PC ratio was increased from 0.20 to 0.45, the average acceleration obtained from the left and right sides of the specimens increased by 11%, while the average displacement reduced by 10%. When FA/PC ratio was increased from 0.45 to 0.70 for the same specimens, the average of acceleration results increased by 12% and displacement results decreased by 8%. In HPFRC beam specimens reinforced with only S fibers, when the FA/PC ratio was increased from 0.20 to 0.45, average acceleration and displacement results increased by 8% and decreased by 9%, respectively. When FA/PC ratio was increased from 0.45 to 0.70, average acceleration and displacement results for the same specimens increased by 10% and decreased by 7%, respectively. When the ratio was increased from 0.20 to 0.45 for specimens with S and P fibers, average acceleration results increased by 16% and displacement results decreased by 10%. When the ratio was increased from 0.45 to 0.70, average acceleration increased by 17% while displacement decreased by 10%. Finally, in the specimens produced with three different fibers, increasing FA/PC ratio from 0.20 to 0.45 caused average acceleration results to increase by 11% and displacement results to decrease by 32%. By increasing FA/PC ratio for the same specimens from 0.45 to 0.70, average acceleration results increased by 25% and displacement results decreased by 18%.

Results clearly show that higher amounts of FA improved the rigidity, acceleration capacity and impact resistance of HPFRC mixtures under sudden loading. It also reduced displacement with impact loading and enhanced resistance to higher rates of acceleration and impact energy. This outcome was valid even for reference specimens without fibers. To be more precise, increased FA was the most effective in increasing acceleration and decreasing displacement for specimens reinforced with three different fibers. The possible explanation for more pronounced impact performance in HPFRC specimens with hybrid fibers and increased FA may be the influence of FA particles in more uniformly distributing individual

fibers due to their spherical surface characteristics and ability to lower matrix fracture toughness results in favor of achieving increased ductility (flexural displacement) (Table 1).

#### **3.2.4 Residual displacement**

In addition to maximum displacement values measured at the first moment of drop hammer impact, the residual displacement values remained on the beam specimens after the completion of impact tests were measured for all specimens as well. Residual displacement values remaining on beam specimens after completion of impact loading are listed in the last column of Table 2. Based on the residual displacement results and typical cracking behavior after impact loading (Figure 7), maximum damage occurred in reference specimens, with an average residual displacement of 27.9 mm for the specimen series with no fibers. Average residual displacement of specimens with only S fibers was very close to that of reference specimens at 27.4 mm. For those incorporating S and P fibers, the value was 15.1 mm, which was 45% smaller than that obtained from specimens without fibers and with only S fibers. Average residual displacement in specimens with three different fibers was 10.67 mm, which was 30% smaller than the values of specimens with S and P fibers. Maximum and residual displacement values were comparably lower in specimens reinforced with P, S and N fibers. These findings demonstrate that HPFRC beams with three different fibers were the least affected by the impact load which were also in line with previously reported results.

#### **3.3 Nonlinear finite element simulation of test specimens**

In the numerical part of the study, an explicit module of the ABAQUS finite element analysis software was used to investigate the behavior of structural members under performed dynamic effects for non-linear analysis. Test setup and specimens were modelled in the software, and element types, material properties, mesh sizes, time steps and boundary were defined. Specimen sizes and support conditions were noted, as in the test program. No external forces were applied to the system, excluding gravitational force. As in the experimental program, the drop height and mass of the steel drop hammer were 600 mm and 9 kg in the analysis, respectively. The element type selected was C3D10M (10-node modified tetrahedron), which gives the best results under dynamic effects. A steel plate was located on the mid-point of specimen to prevent local crushing from the point of impact loading. Finite element models were created after completing the node and element numbers of the test specimen, hammer and steel plate. Since specimen sizes were the same, the same node and element numbers were defined in the software. Impact load should be transferred completely to the specimen for the consistency between experimental and numerical studies. For this

reason, each model is analyzed for different increment sizes and impact moment of the hammer to the specimen is determined.

Material properties were assigned to the related geometries in the software. The software's concrete damage plasticity model was used to define non-linear behavior of concrete material. Linear elastic material models were defined for the steel hammer and plate, as presented in Table 3. Properties of HPFRC mixtures changed, since the material properties and fractions of ingredients in the mixtures were relatively different. As a result of tests performed on HPFRC mixtures used in producing beam specimens, compressive stress-strain and uniaxial tensile stress-strain graphs of each mixture were obtained experimentally. In the finite element analysis, material models obtained separately for each beam specimen in both compression and uniaxial tensile stress-strain were used and entered into the ABAQUS software as raw data. Examples selected from material models used in the analysis of test specimens are shown in Figure 8 and 9 for compressive and uniaxial tensile stresses, respectively.

After material properties were assigned to the related geometries, analysis type was determined. Here, C3D10M elements which are compatible with contact problems were used in the analysis. These members can only be utilized in explicit solutions. After deciding the analysis type, time steps and time spans were defined in the software and time increments were assigned for each drop movement of the hammer. As the analysis was an incremental dynamic one, it was performed for short time intervals to reach the proper results. So, time increment was selected as  $2 \times 10^{-8}$  s when the hammer started to apply loading to the test specimen.

Mesh structure of the model is determined according to the element and analysis types. Based on a comparative and sensitivity analysis of results between 10 and 30 mm mesh sizes, 15 mm mesh was chosen. Fixed supports were defined for each end of the specimen. On the other hand, the steel hammer was modelled to enable the vertical movement only and horizontal movement of the hammer is restrained.

Contact between the hammer and specimen was modelled by defining contact surfaces. For this purpose, surface to surface contact was selected between the steel hammer and test specimen. Surface of the hammer applying the impact load was chosen as master, and the corresponding part of the specimen was chosen as slave. Tangential and normal behavior contact properties were selected in the software to model contact between the hammer and specimen. Since friction effects occurred during the experimental program, the coefficient of friction for contact surfaces was taken as 0.02 in tangential behavior. On the other hand,

rebound movement of the hammer from the specimen was modelled by normal contact behavior.

A finite elements' analysis was performed for each test specimen. Few test specimens were initially used to calibrate various unmeasured coefficients; for example concrete damage plasticity model coefficients and friction coefficient for contact surface between the hammer and specimen. Acceleration, displacement, impact load and residual displacements were obtained for various test specimens. Figure 10 shows maximum acceleration vs. time, displacement vs. time and impact load vs. time graphs from numerical and experimental works for specimens of P1S1N0\_0.45\_1.0 mixture (Mixture #8). Graphs were obtained for a single drop of the steel hammer so results from the analysis could be compared with the test results. Maximum results obtained from the analysis for all test specimens are summarized in Table 4.

When the results presented in Table 4 are evaluated, it is evident that maximum acceleration ratios obtained from actual experiments and finite element analysis range between 0.80 and 1.10. Maximum displacement ratios obtained from the experiments and finite element analysis range between 0.84 and 1.13. The ratios of residual displacements obtained from the experiments and finite element analysis range between 0.86 and 1.25. These findings clearly show that results of ABAQUS analysis are in good agreement with the experimental results, confirming the validity of the proposed model.

Von-Misses stress distributions for three test specimens were determined and plotted Figure 11. High tensile stresses and cracks occurred around the impact load point for all test specimens. Deformed specimen shapes for the same three specimens were also determined and presented in Figure 11. Cracks and distributed damage monitored after the actual experiments were in agreement with figures acquired as a result of the non-linear finite element analysis. Maximum displacements for the three specimens were observed close to the mid-point where the impact loading was applied, similar to that observed in laboratory experiments.

#### 4. CONCLUSIONS

This research evaluated the impact resistance of beam specimens produced with deflection-hardening HPFRC mixtures after free-fall drop-weight tests. Primary importance was given to observing the effects of three main variables (types/amounts of fiber reinforcement, A/B ratio and FA/PC ratio) on the impact behavior of HPFRC beams. To do so, acceleration, displacement and impact load vs. time graphs were experimentally obtained and analyzed for HPFRC beam specimens. Furthermore, tested beam specimens were modelled in a finite

element program (ABAQUS) and incremental nonlinear dynamic analyses were performed. Finally, results obtained from the laboratory experiments were compared with those obtained from the numerical study. Following conclusions were drawn:

- Fiber reinforcement was significantly effective in improving the impact resistance of reference HPFRC mixtures without fibers for a given FA/PC and A/B ratio. Increasing the dosage of fibers improved the impact resistance of HPFRC mixtures so that after the introduction of impact loading, smaller flexural displacements were obtained from beam specimens with two (S, P, by 2% volume) and three (S, P, N, by 2% volume) different fibers compared to specimens with only S (by 1% volume) fibers. At the same fiber dosage, FA/PC ratio and A/B ratio, better impact performances were noted from HPFRC beam specimens hybridized with three different fibers (S, P, N) than the ones with two different fibers (S, P) which showed that costly P fibers can safely be replaced with cheaper N fibers without risking mechanical properties in favor of achieving enhanced impact resistance.
- Increased A/B ratios resulted in reduced impact resistance of HPFRC beam specimens with hybrid fibers for a given FA/PC ratio and fiber dosage. However, the rates of decrement were not that pronounced even when A/B ratio was doubled from 1.0 to 2.0. It is possible that a different impact behavior (more enhanced) can be obtained in the presence of relatively high amounts of coarse aggregates when the cross-sectional area of impact, which was relatively small ( $50 \times 50 \text{ mm}^2$ ) herein, is modified. Increasing the amounts of coarse aggregates without sacrificing the mechanical properties and impact resistance can be very beneficial for minimizing the dimensional stability problems and shrinkage-related cracking potential of HPFRC mixtures.
- Improved impact performance was obtained when the FA/PC ratios of HPFRC mixtures were increased and this was irrespective of the A/B ratio and fiber type/dosage. Increased utilization rates of Class-F fly ash seem to improve the workability of fresh mixtures, increase the fiber distribution and reduce matrix fracture toughness in favor of achieving higher flexural displacement and resultingly, enhanced impact performance.
- ABAQUS finite element software, used for the purposes of numerical analysis, was successful in modeling impact behavior of HPFRC beam specimens; acceleration, displacement and residual displacement results obtained from both experimental and numerical studies were in good agreement. Moreover, beam displacement profiles and stress distributions that were calculated from the numerical analysis were found to be in line with the experimental results. The effects of experimental variables on the displacement results



were concordant with the numerical analysis, confirming that ABAQUS program can be used in the design process of proposed HPFRC mixtures before implementing actual tests. Overall, the findings of current study reveal the actual producibility of deflection-hardening HPFRC mixtures with multiple microcracking and improved impact resistance in the presence of large share of coarse aggregates. Although the study will serve as a benchmark for the implementation of further studies in the future and make such materials to be used in actual field conditions at more reasonable prices, more elaborated studies taking into account additional variant parameters in materials' properties/testing procedure (including different specimen dimensions, fiber types/amounts, levels of impact loading etc.) are necessary for a more precise understanding of HPFRCs under impact loading.

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**TABLE 1** Ingredients used for the production of mixtures (units are in kg/m<sup>3</sup>) and basic mechanical property results after 28 days

Mixture					Aggregates		Water	HRWRA	Fibers			Mechanical Properties		
#	ID	PC	FA	SF	Fine	Coarse			P	S	N	Comp. St. (MPa)	Flex. St. (MPa)	Flex. Dis. (mm)
1	P0S0N0_0.20_1.0	690	138	48	495	380	351	-	-	-	-	50.6	3.20	0.22
2	P0S0N0_0.45_1.0	567	255	40	488	375	345	-	-	-	-	40.2	3.50	0.20
3	P0S0N0_0.70_1.0	481	337	34	483	372	341	-	-	-	-	31.3	3.00	0.20
4	P0S1N0_0.20_1.0	683	137	48	490	376	347	0.6	-	78	-	47.9	6.00	1.60
5	P0S1N0_0.45_1.0	562	253	39	482	370	342	0.5	-	78	-	48.5	5.48	1.49
6	P0S1N0_0.70_1.0	477	334	33	477	367	338	0.4	-	78	-	35.6	4.68	1.43
7	P1S1N0_0.20_1.0	675	135	47	486	374	343	0.9	13	78	-	52.9	5.88	1.93
8	P1S1N0_0.45_1.0	555	250	39	479	368	337	0.8	13	78	-	44.6	7.95	1.75
9	P1S1N0_0.70_1.0	472	330	33	472	363	334	0.5	13	78	-	38.1	7.58	1.58
10	P1S1N0_0.20_1.5	579	116	41	622	478	294	1.8	13	78	-	55.0	8.83	1.13
11	P1S1N0_0.45_1.5	477	215	33	614	472	290	1.5	13	78	-	44.6	8.03	1.38
12	P1S1N0_0.70_1.5	405	284	28	610	469	287	1.2	13	78	-	38.0	8.40	1.52
13	P1S1N0_0.20_2.0	505	101	35	726	559	257	1.9	13	78	-	56.8	7.05	1.33
14	P1S1N0_0.45_2.0	417	188	29	718	552	254	1.8	13	78	-	48.6	8.55	1.63
15	P1S1N0_0.70_2.0	356	249	25	711	547	252	1.6	13	78	-	43.6	7.48	1.23
16	P0.5S1N0.5_0.20_1.0	675	135	47	486	374	343	1.0	6.5	78	5.7	51.9	6.27	1.47
17	P0.5S1N0.5_0.45_1.0	555	250	39	479	368	337	0.8	6.5	78	5.7	45.4	7.20	1.70
18	P0.5S1N0.5_0.70_1.0	472	330	33	472	363	334	0.7	6.5	78	5.7	40.9	6.60	1.77
19	P0.5S1N0.5_0.20_1.5	578	116	40	623	479	294	3.5	6.5	78	5.7	60.2	6.98	1.30
20	P0.5S1N0.5_0.45_1.5	477	215	33	614	472	290	3.3	6.5	78	5.7	54.5	8.45	1.78
21	P0.5S1N0.5_0.70_1.5	405	284	28	610	469	287	3.0	6.5	78	5.7	46.9	7.03	1.83
22	P0.5S1N0.5_0.20_2.0	505	101	35	726	559	257	5.0	6.5	78	5.7	60.4	8.30	1.43
23	P0.5S1N0.5_0.45_2.0	417	188	29	718	552	254	4.9	6.5	78	5.7	56.3	7.13	1.27
24	P0.5S1N0.5_0.70_2.0	355	249	25	712	548	251	4.8	6.5	78	5.7	51.0	7.78	1.68

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**TABLE 2** Free fall drop-weight test results

Mix. No	Mix. ID	Acceleration – g (m/s <sup>2</sup> )				Displacement (mm)		Impact Load (kN)	Residual Displacement (mm)
		Left		Right		Left	Right		
		Max.	Min.	Max.	Min.				
1	P0S0N0_0.20_1.0	120.0	-211.6	122.4	-319.5	-44.1	-44.7	13.8	28.5
2	P0S0N0_0.45_1.0	132.0	-118.2	140.0	-139.9	-40.8	-39.1	12.3	30.1
3	P0S0N0_0.70_1.0	152.3	-533.1	156.0	-418.3	-36.8	-36.8	12.3	24.9
4	P0S1N0_0.20_1.0	188.0	-303.2	187.3	-331.7	-34.8	-33.2	12.0	27.1
5	P0S1N0_0.45_1.0	205.1	-490.3	204.1	-276.4	-31.4	-30.2	12.3	27.3
6	P0S1N0_0.70_1.0	227.2	-284.0	225.3	-377.5	-29.6	-27.9	12.3	27.8
7	P1S1N0_0.20_1.0	216.1	-334.2	223.4	-265.5	-25.9	-27.6	12.2	19.8
8	P1S1N0_0.45_1.0	258.7	-557.0	267.4	-442.2	-21.3	-25.3	11.1	11.8
9	P1S1N0_0.70_1.0	319.5	-372.0	327.1	-552.8	-20.3	-22.8	12.4	11.8
10	P1S1N0_0.20_1.5	263.0	-262.9	261.2	-260.9	-29.1	-31.4	14.5	13.4
11	P1S1N0_0.45_1.5	323.1	-323.0	321.0	-289.3	-26.5	-28.1	12.5	14.0
12	P1S1N0_0.70_1.5	398.0	-397.9	339.7	-395.0	-22.6	-24.5	14.7	12.8
13	P1S1N0_0.20_2.0	293.2	-557.0	300.4	-485.1	-30.6	-32.4	14.6	16.8
14	P1S1N0_0.45_2.0	356.7	-445.6	334.8	-531.0	-28.8	-30.4	12.1	15.6
15	P1S1N0_0.70_2.0	423.4	-423.3	431.6	-540.6	-26.6	-27.8	12.9	20.1
16	P0.5S1N0.5_0.20_1.0	300.9	-512.4	315.4	-342.7	-19.4	-17.1	12.2	14.3
17	P0.5S1N0.5_0.45_1.0	349.5	-902.3	350.0	-491.4	-12.8	-12.1	12.5	5.49
18	P0.5S1N0.5_0.70_1.0	471.9	-557.0	473.7	-552.8	-10.3	-10.9	12.2	4.89
19	P0.5S1N0.5_0.20_1.5	376.4	-557.0	388.9	-546.0	-22.2	-21.4	12.2	16.6
20	P0.5S1N0.5_0.45_1.5	429.1	-662.8	432.4	-417.4	-14.8	-15.6	12.2	9.26
21	P0.5S1N0.5_0.70_1.5	572.3	-983.0	571.8	-1233	-12.1	-11.4	12.7	8.07
22	P0.5S1N0.5_0.20_2.0	421.7	-421.6	423.3	-818.1	-24.4	-24.8	12.3	19.2
23	P0.5S1N0.5_0.45_2.0	475.9	-1175	466.0	-1166	-16.2	-16.2	12.8	10.1
24	P0.5S1N0.5_0.70_2.0	618.9	-1164	619.8	619.1	-13.3	-13.4	12.2	8.17

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**TABLE 3** Material properties of steel hammer and plate used for finite element analysis

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model

Property	Steel hammer and plate
Weight per unit of volume (kg/m <sup>3</sup> )	7850
Modulus of elasticity (MPa)	200000
Poisson's ratio	0.30
Shear modulus (MPa)	76923
Bulk modulus (MPa)	166670

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**TABLE 4** Comparison of experimental and numerical results

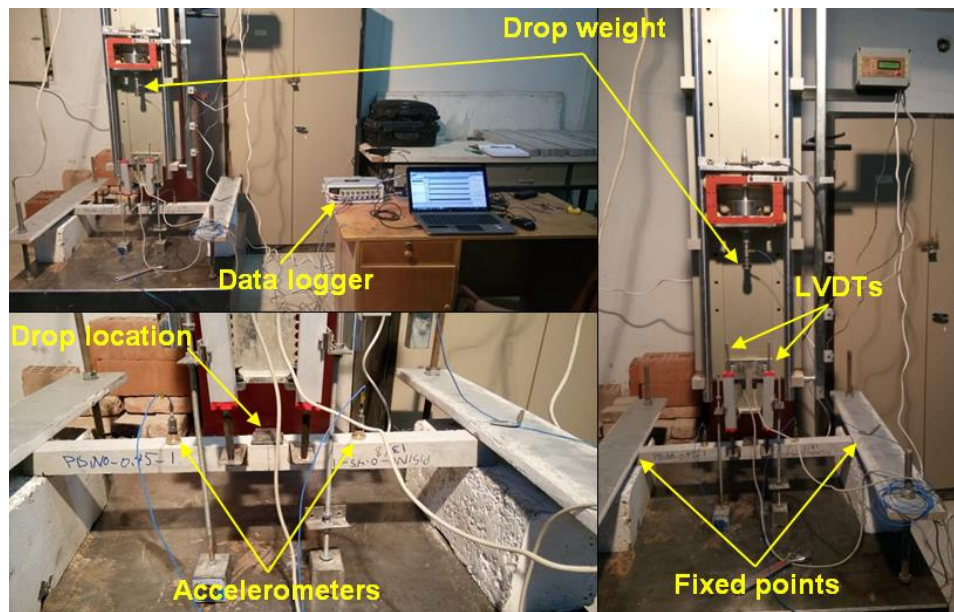
Mix. No	Mix. ID	Left Acceleration – g (m/s <sup>2</sup> )					Left Displacement (mm)			Impact Load (kN)			Residual Displacement (mm)		
		Exp.		ABAQUS		Ratio <sup>1</sup>	Exp.		Ratio <sup>2</sup>	Exp.		Ratio <sup>3</sup>	Exp.		Ratio <sup>4</sup>
		Max.	Min.	Max.	Min.		Max.	Min.		Max.	Min.		Max.	Min.	
1	P0S0N0_0.20_1.0	120.0	-211.6	122.1	-181.5	0.98	-44.1	-48.2	0.91	13.8	15.6	0.88	28.5	24.2	1.18
2	P0S0N0_0.45_1.0	132.0	-118.2	131.5	-148.3	1.00	-40.8	-43.3	0.94	12.3	14.6	0.84	30.1	27.3	1.11
3	P0S0N0_0.70_1.0	152.3	-533.1	174.6	-203.4	0.87	-36.8	-40.0	0.92	12.3	15.0	0.82	24.9	21.5	1.16
4	P0S1N0_0.20_1.0	188.1	-303.2	235.2	-197.5	0.80	-34.8	-37.2	0.93	12.0	13.9	0.87	27.1	25.0	1.08
5	P0S1N0_0.45_1.0	205.1	-490.3	254.9	-301.4	0.80	-31.4	-34.2	0.92	12.3	14.4	0.86	27.3	24.7	1.10
6	P0S1N0_0.70_1.0	227.2	-284.0	266.8	-227.5	0.85	-29.6	-33.2	0.89	12.3	14.0	0.88	27.8	22.2	1.25
7	P1S1N0_0.20_1.0	216.1	-334.2	224.8	-277.6	0.96	-25.9	-28.5	0.91	12.2	13.3	0.92	19.8	16.2	1.22
8	P1S1N0_0.45_1.0	258.7	-557.0	297.7	-366.4	0.87	-21.3	-23.1	0.92	11.1	12.6	0.88	11.8	13.8	0.86
9	P1S1N0_0.70_1.0	319.5	-372.0	304.6	-351.7	1.05	-20.3	-23.5	0.87	12.4	12.5	0.99	11.8	12.4	0.96
10	P1S1N0_0.20_1.5	263.0	-262.9	286.2	241.6	0.92	-29.1	-27.6	1.05	14.5	13.9	1.04	13.4	12.9	1.04
11	P1S1N0_0.45_1.5	323.1	-323.0	293.8	-277.2	1.10	-26.5	-26.6	1.00	12.5	13.8	0.91	14.0	13.3	1.06
12	P1S1N0_0.70_1.5	398.1	-397.9	371.7	-344.3	1.07	-22.6	-25.8	0.87	14.7	14.6	1.00	12.9	12.2	1.06
13	P1S1N0_0.20_2.0	293.2	-557.0	327.7	-389.2	0.89	-30.6	-28.8	1.06	14.6	14.9	0.98	16.8	13.6	1.23
14	P1S1N0_0.45_2.0	356.7	-445.6	344.6	-373.5	1.04	-28.8	-30.3	0.95	12.1	13.5	0.89	15.6	13.5	1.16
15	P1S1N0_0.70_2.0	423.4	-423.3	413.5	-379.5	1.02	-26.6	-28.4	0.94	13.0	13.2	0.98	20.1	17.6	1.14
16	P0.5S1N0.5_0.20_1.0	300.9	-512.4	354.4	-378.3	0.85	-19.4	-20.3	0.95	12.2	13.2	0.93	14.3	12.2	1.17
17	P0.5S1N0.5_0.45_1.0	349.5	-902.3	366.1	-443.2	0.95	-12.8	-14.2	0.90	12.5	13.1	0.95	5.50	5.70	0.96
18	P0.5S1N0.5_0.70_1.0	471.9	-557.0	475.6	-403.2	0.99	-10.3	-10.0	1.03	12.2	12.7	0.96	4.90	4.60	1.07
19	P0.5S1N0.5_0.20_1.5	376.4	-557.0	381.4	-438.5	0.99	-22.2	-19.7	1.13	12.2	13.0	0.94	16.6	13.9	1.20
20	P0.5S1N0.5_0.45_1.5	429.1	-662.8	398.7	-442.5	1.08	-14.8	-17.4	0.85	12.2	12.9	0.95	9.30	10.6	0.87
21	P0.5S1N0.5_0.70_1.5	572.3	-983.0	525.9	-418.4	1.09	-12.1	-13.5	0.90	12.7	14.0	0.91	8.10	9.40	0.86
22	P0.5S1N0.5_0.20_2.0	421.7	-421.6	419.6	-441.8	1.01	-24.4	-21.5	1.13	12.3	13.2	0.93	19.2	16.8	1.14
23	P0.5S1N0.5_0.45_2.0	475.9	-1175	433.9	-479.6	1.10	-16.2	-17.5	0.92	12.8	14.0	0.91	10.1	9.90	1.02
24	P0.5S1N0.5_0.70_2.0	618.9	-1164	601.3	-473.5	1.03	-13.3	-15.8	0.84	12.2	13.1	0.93	8.20	9.60	0.86

744 <sup>1</sup> Ratio of left experimental maximum acceleration to numerical maximum acceleration values745 <sup>2</sup> Ratio of left experimental displacement to numerical maximum displacement values746 <sup>3</sup> Ratio of experimental impact load to numerical impact load values747 <sup>4</sup> Ratio of experimental residual displacement to numerical residual displacement values

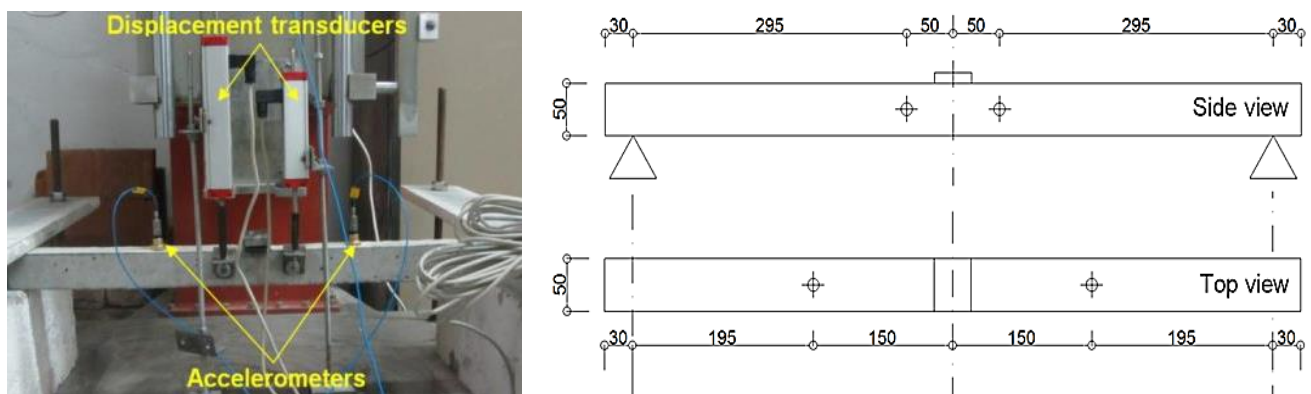
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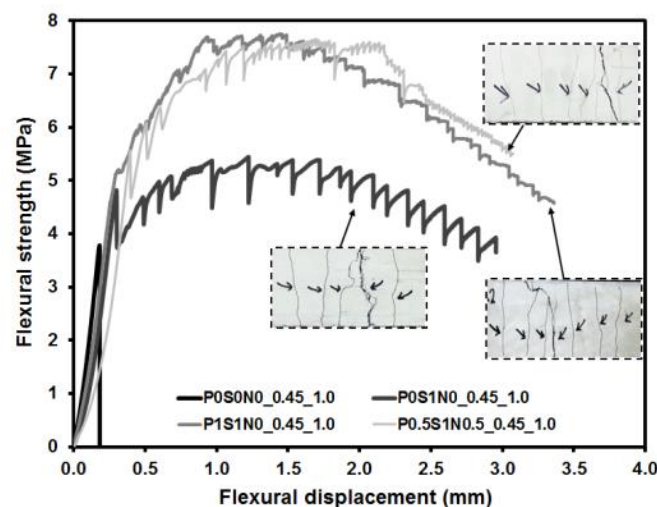




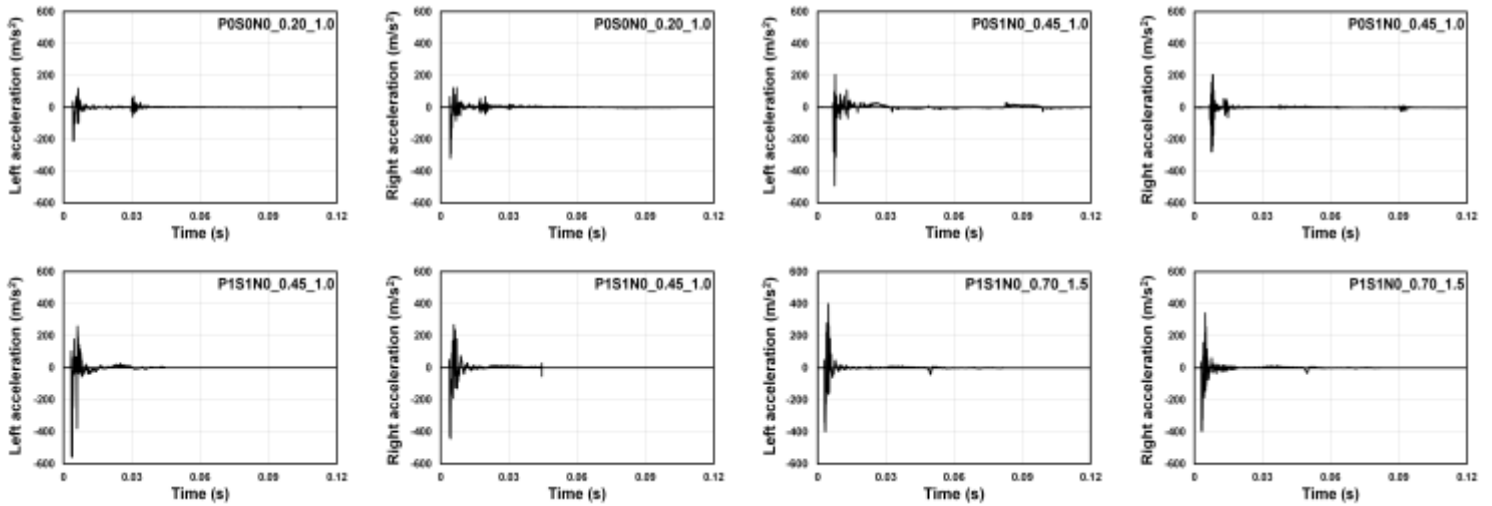
**FIGURE 1** Free fall drop-weight test setup and view of beam specimen



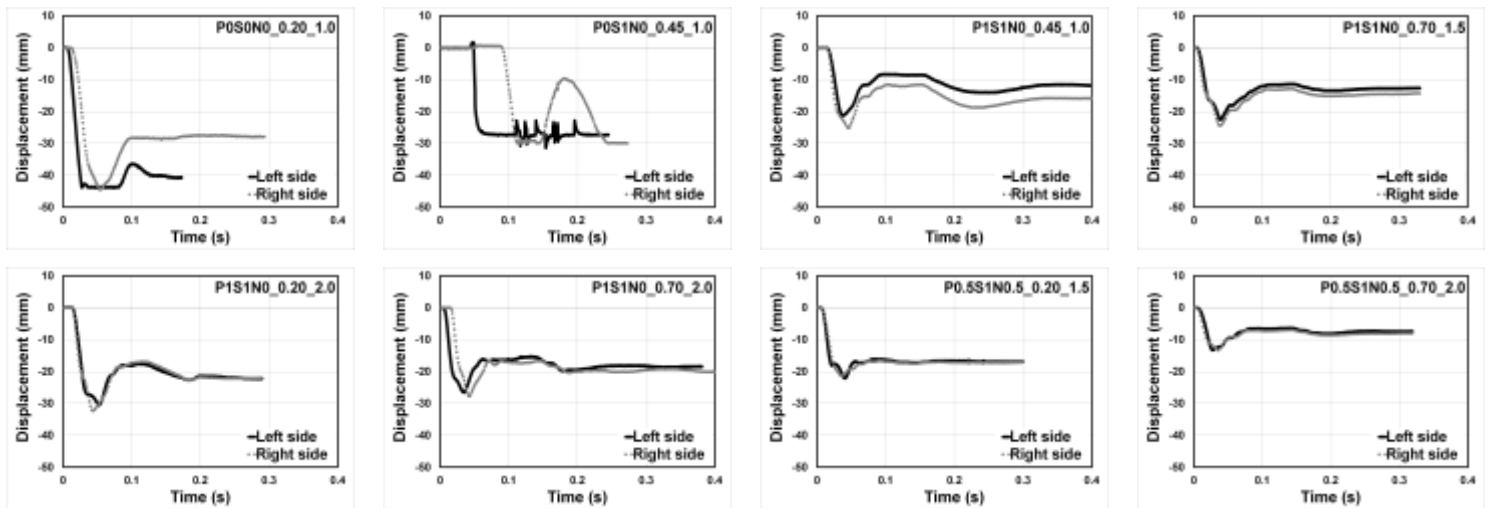
**FIGURE 2** View of beam specimen ready for impact testing and impact test layout (all dimensions are in mm)



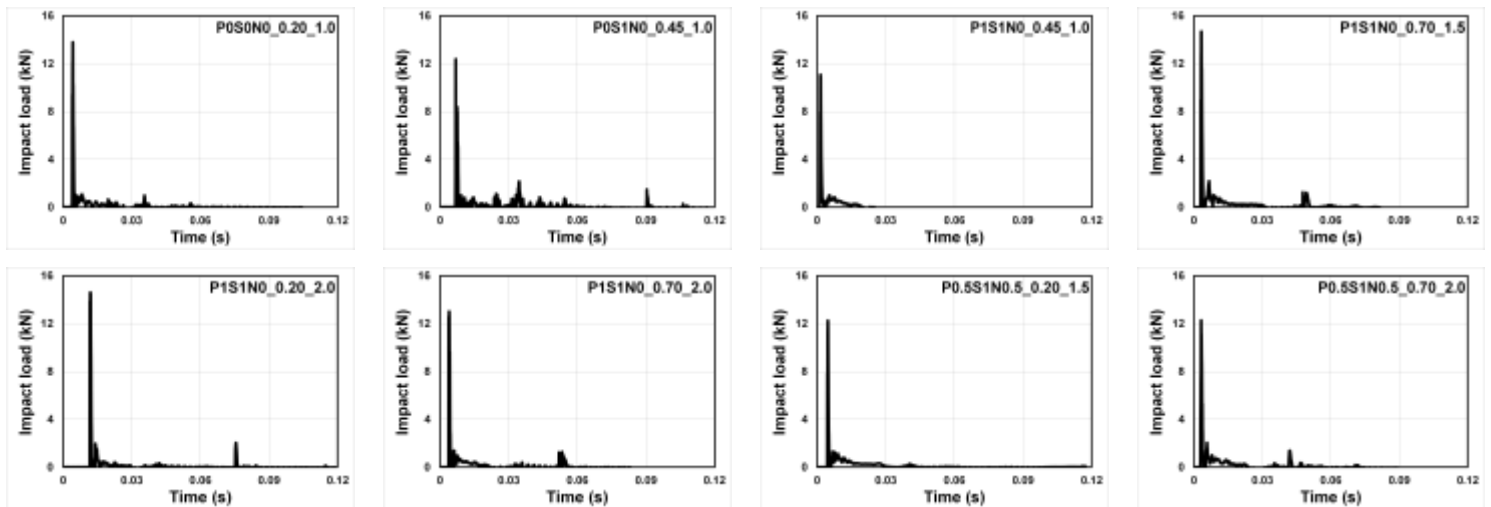
**FIGURE 3** Effects of utilization of different types/dosages of fibers on typical flexural strength – displacement graphs and multiple microcracking behaviors of specimens



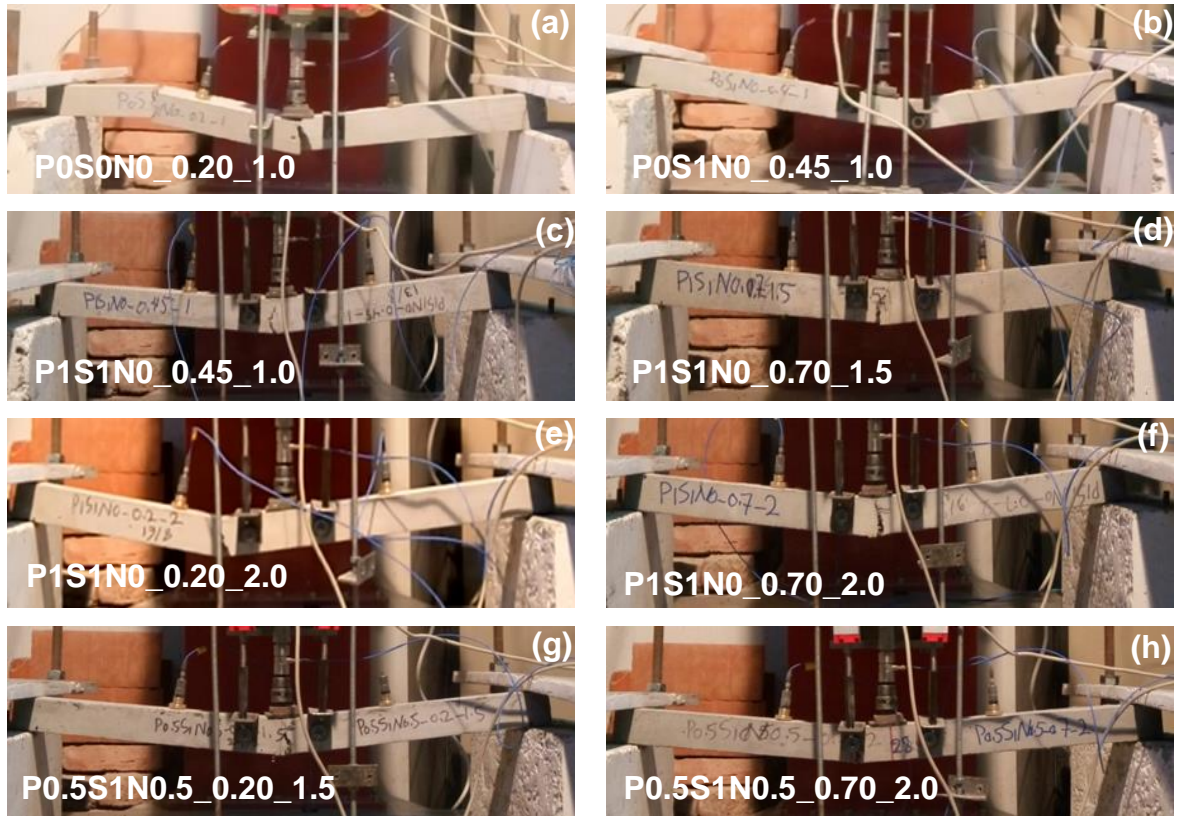
758 **FIGURE 4** Representative acceleration vs. time graphs for selected specimens from different  
 759 mixtures



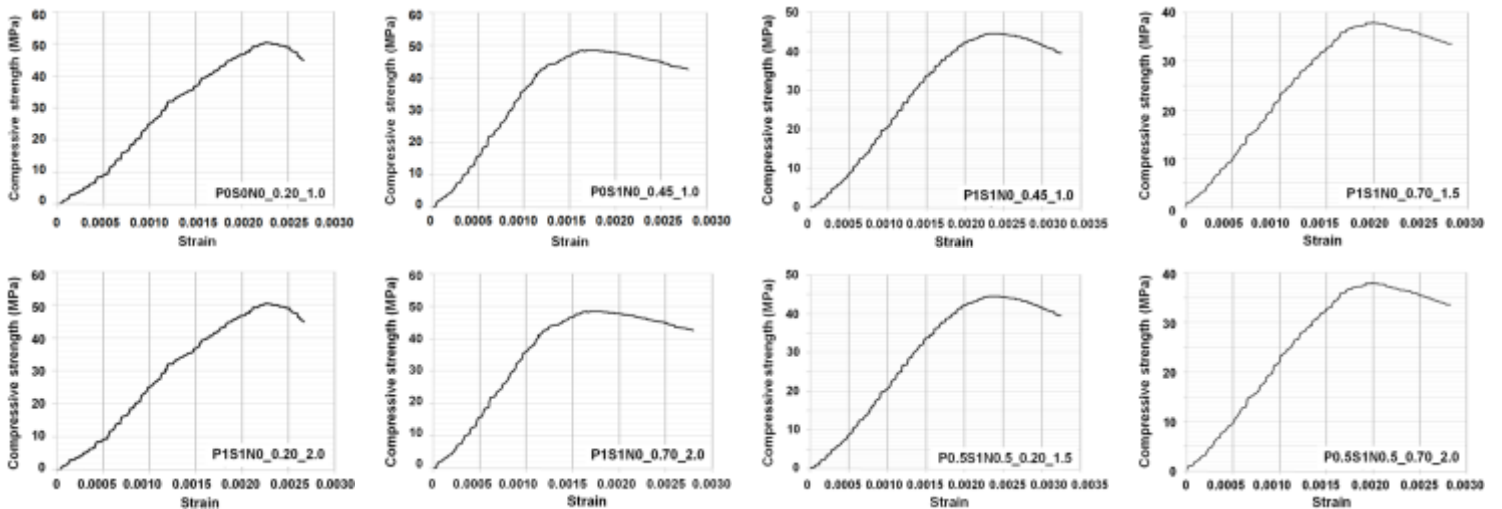
760 **FIGURE 5** Representative displacement vs. time graphs for selected specimens from  
 761 different mixtures



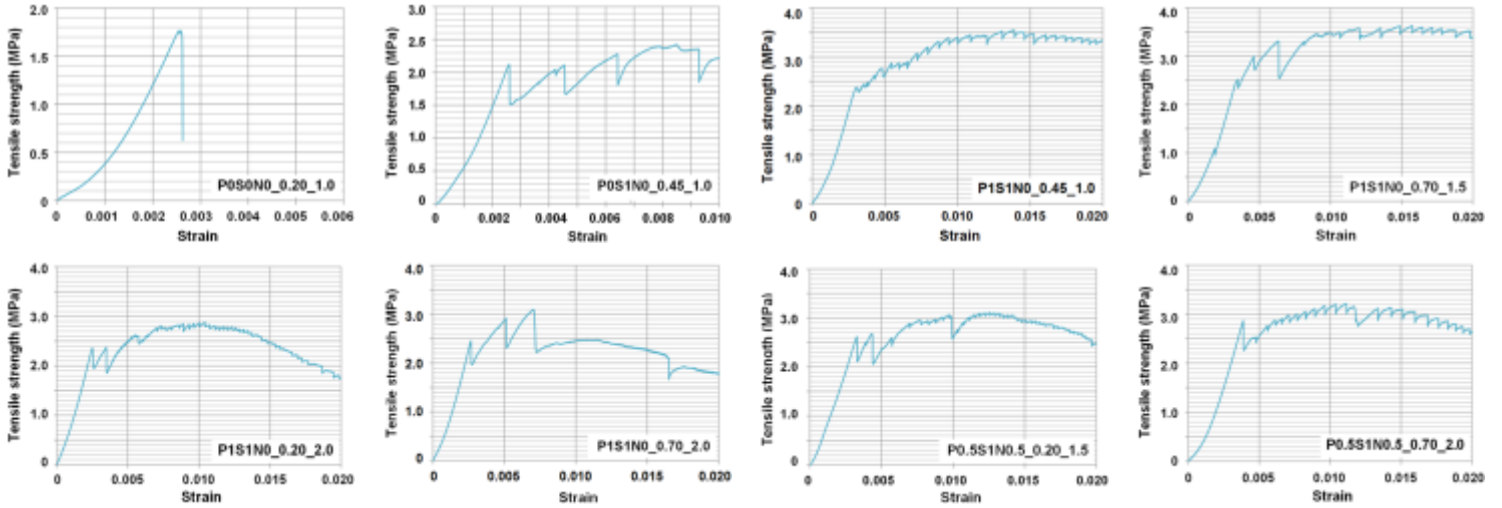
762 **FIGURE 6** Representative impact load vs. time graphs for selected specimens from different  
 763 mixtures



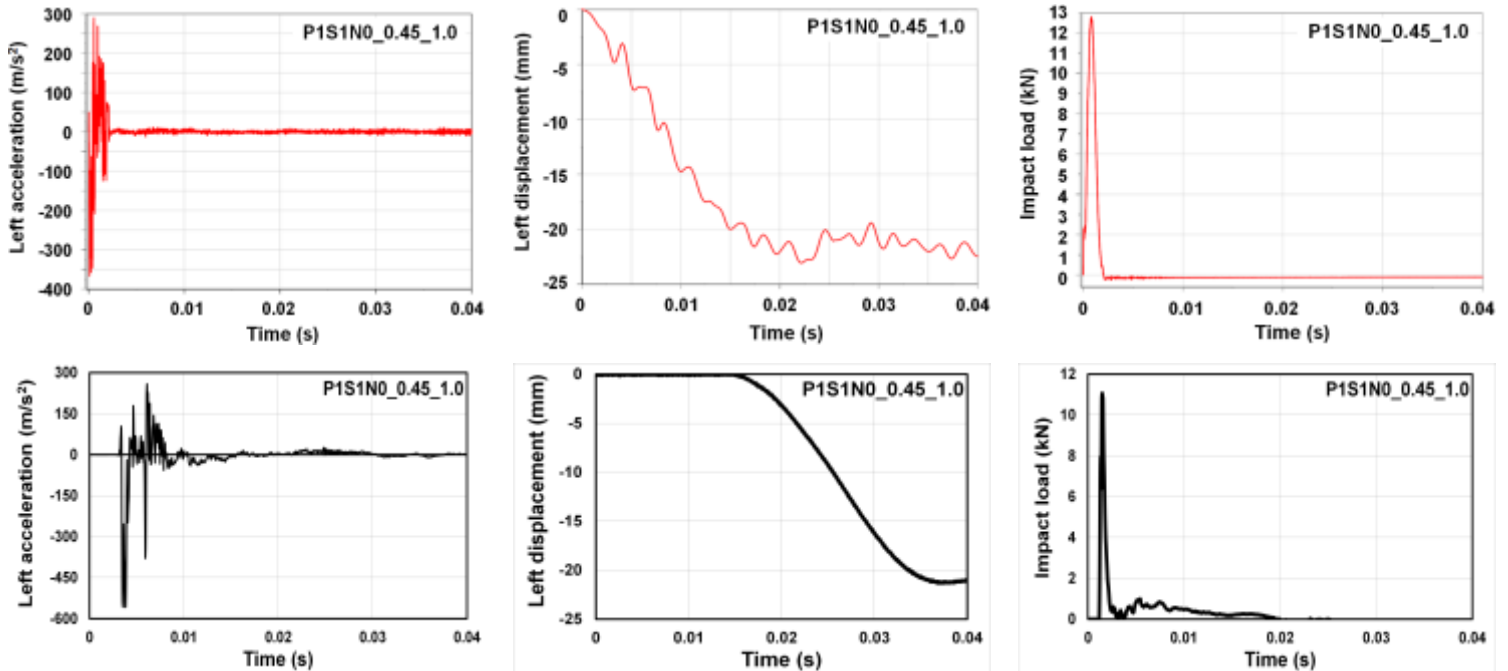
**FIGURE 7** Representantive views of the specimens from different mixtures after final failure



**FIGURE 8** Representantive compressive stress vs. strain models of specimens from different mixtures for FEA model

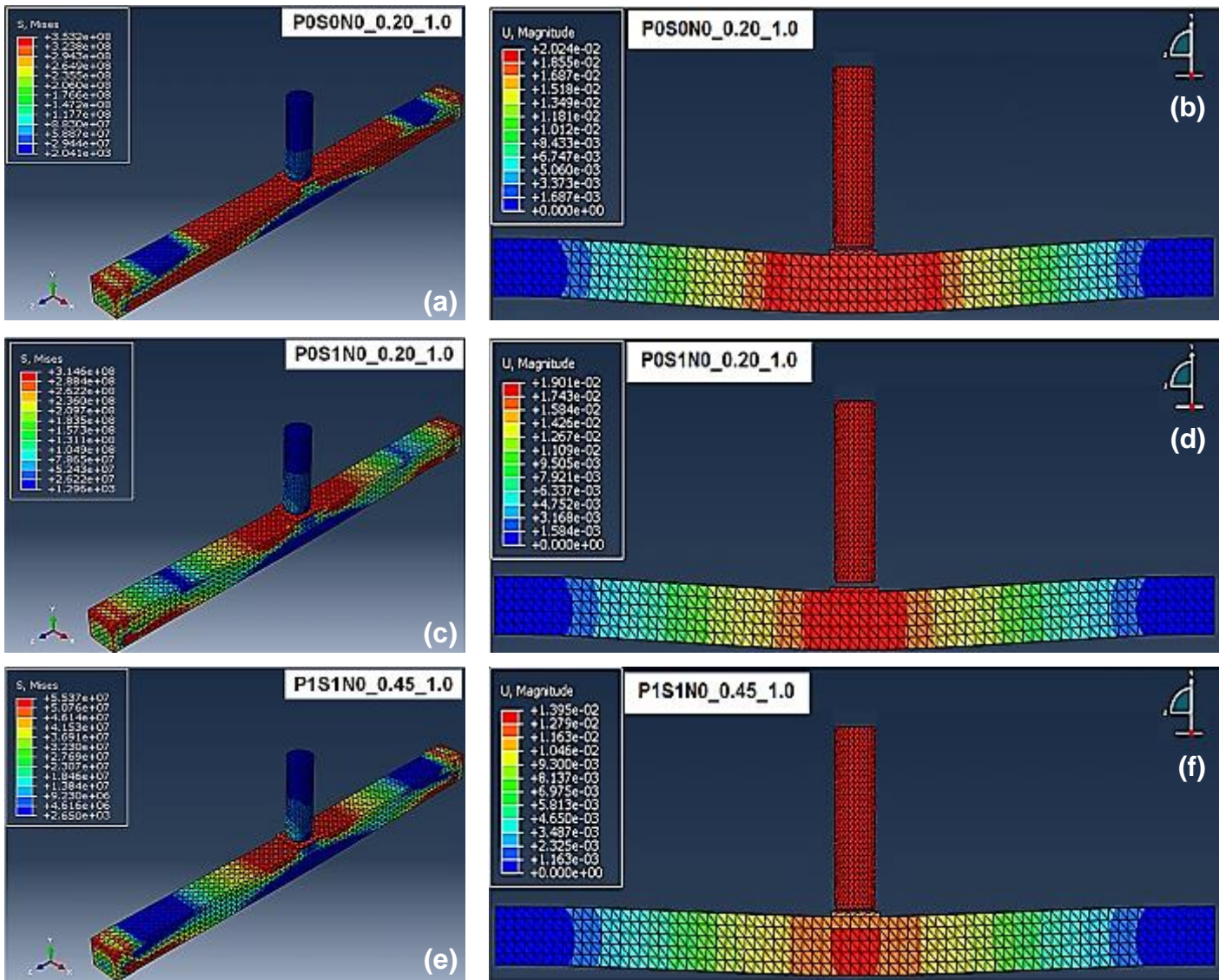


**FIGURE 9** Representative uniaxial tensile stress vs. strain models of specimens from different mixtures for FEA model



**FIGURE 10** Acceleration vs. time, displacement vs. time and impact load vs. time graphs of specimens of P1S1N0\_0.45\_1.0 (Mixture #8) obtained from finite element analysis at the top and from real-time experiments at the bottom





786 **FIGURE 11** Representantive stress distributions (on the left) and deformed shapes (on the  
787 stress distributions (on the left) and deformed shapes (on the right) of specimens from different mixtures during impact